

B. B. S. S. Sec School
CLASS-8 (MATHS)

(1)

Irrational numbers:- A number which can not be written in the form of $\frac{p}{q}$ ($q \neq 0$) where p and q are integers. for example, $\sqrt{2}, \sqrt{3}, \sqrt[3]{5}, \pi$ etc are irrational numbers.

Theorem:-

Let p be a prime number, if p divides a^2 then p divides a , where a is a positive integer.

If p is a prime number then \sqrt{p} is an irrational number.

To prove a number be irrational:-

Working Rules:-

Step I:- Assume the number, to the contrary as rational.

Step II Based on this assumption, write a series of statements which are logically correct.

Step III Finally, conclude the statement which contradicts the assumption that given number be rational therefore assumption must be wrong. Hence given number is irrational.

Ex. 1.3:- Q.1 Let $\sqrt{5}$ be rational,
 $\therefore \sqrt{5} = \frac{a}{b}$ ($b \neq 0$) where a and b are coprimes.

$$\Rightarrow a = \sqrt{5}b$$

on squaring both sides we get

$$a^2 = 5b^2 \quad \text{--- (1)}$$

$\Rightarrow a^2$ is divisible by 5

$\Rightarrow a$ is divisible by 5

$\therefore 5$ is a factor of a

Let $a = 5c$

on squaring both sides

$$a^2 = 25c^2 \quad \text{--- (1)}$$

Now from (1) and (1),

$$5b^2 = 25c^2$$

$$b^2 = \frac{25}{5} c^2 = 5c^2$$

$$\Rightarrow b^2 = 5c^2$$

$\Rightarrow b^2$ is divisible by 5

$\Rightarrow b$ is divisible by 5

$\therefore 5$ is a factor of b .

This shows that a and b have a common factor of 5

but we have assumed that a and b are co-primes

So, our assumption is wrong

$\therefore \sqrt{5}$ is irrational. HP

Q.2. Let $3 + 2\sqrt{5}$ is rational, therefore

$$3 + 2\sqrt{5} = \frac{a}{b} \quad (b \neq 0) \text{ where } a \text{ and } b \text{ are co-primes.}$$

$$2\sqrt{5} = \frac{a}{b} - 3$$

$$2\sqrt{5} = \frac{a - 3b}{b}$$

$$\sqrt{5} = \frac{a - 3b}{2b}$$

$\therefore \frac{a - 3b}{2b}$ is rational because a and b are integers.

$\therefore \sqrt{5}$ is rational.

But we know that $\sqrt{5}$ is irrational. Therefore our assumption is wrong and hence $3 + 2\sqrt{5}$ is Irrational. HP

Home work. Ex 1.3 Q. 3 (i) (ii) (iii)

Assignment:-

(1) Prove that $\sqrt{3}$ is irrational.

(2) Prove that $5 + 3\sqrt{7}$ is irrational.

(3) Prove that $\frac{1}{\sqrt{3}}$ is irrational.

(4) Prove that $3 - 5\sqrt{2}$ is irrational.

Theorem:- (i) If x is a rational number whose decimal expansion terminates, then x can be expressed in the form of $\frac{p}{q}$, where p and q are co-primes (no factor other than 1) and the prime factorisation of q is of the form $2^m 5^n$ where m and n are non negative integers.

(ii) Let $x = \frac{p}{q}$ be a rational number. Such that the prime factorisation of q is not of the form $2^m 5^n$ where n and m are non negative integers. Then x has a decimal expansion which is non terminating and repeating.

Ex 1.4 Q1

(i) $\frac{13}{3125}$ Here $q = 3125$

$$q = 3125 = 5 \times 5 \times 5 \times 5 \times 5 = 5^5$$

$$\Rightarrow 3125 = 2^0 5^5$$

Here q is in the form of $2^m 5^n$ where $m=0, n=5$

\therefore Decimal expansion is terminated.

$$\begin{array}{r} 5 \overline{) 3125} \\ \underline{5} \\ 625 \\ \underline{5} \\ 125 \\ \underline{5} \\ 25 \\ \underline{5} \\ 5 \\ \underline{5} \\ 1 \end{array}$$

(iii) $\frac{64}{455}$, $q = 455$

$$q = 5 \times 7 \times 13$$

q is not in the form of $2^m 5^n$

\therefore Decimal expansion is non terminating

$$\begin{array}{r} 5 \overline{) 455} \\ \underline{5} \\ 91 \\ \underline{7} \\ 13 \\ \underline{13} \\ 1 \end{array}$$

Q.2 (i)

$$\frac{13}{3125} = \frac{13}{5 \times 5 \times 5 \times 5 \times 5} = \frac{13}{5^5} = \frac{13 \times 2^5}{5^5 \times 2^5} = \frac{13 \times 32}{10^5} = \frac{416}{100000} = 0.00416 \text{ Ans}$$

(ii) $\frac{15}{1600} = \frac{3 \times 5}{2^6 \times 5 \times 2} = \frac{3}{2^6 \times 5} = \frac{3 \times 5^5}{2^6 \times 5 \times 5^5} = \frac{9375}{2^6 \times 5^6} = \frac{9375}{10^6} = 0.009375 \text{ Ans}$

P.T.O

Q.3 (i) $\therefore 43.123456789$ is terminating
 \therefore It represents a rational number.

(4)

43.123456789 can be expressed in the form of $\frac{p}{q}$
where $q = 10^9$.

(ii) $0.120120012000\dots$ is non-terminating and non-repeating
 \therefore It is an irrational number.

Home work: Ex. 1.4 Q1. (i) (iv) to (x)

Q2. (i) (ii) (v) to (x)

Q3 (iii)

Assignment:

Q1 without actual division state whether the following rational number will have a terminating or a non-terminating repeating decimal expansion.

(i) $\frac{17}{8}$ (ii) $\frac{53}{343}$ (iii) $\frac{17}{625}$ (iv) $\frac{77}{210}$ (v) $\frac{17}{320}$ (vi) $\frac{23}{2^3 \cdot 5^2}$

Q2 After how many decimal expansion will the following expansion terminate.

(i) $\frac{35}{16000}$ (ii) $\frac{13}{125}$ (iii) $\frac{43}{2^4 \times 5^3}$ (iv) $\frac{107}{1250}$

Q.3 Find HCF and LCM of.

(i) 615, 750 (ii) 81, 54 (iii) 1250, 31575

Q.4 Given the HCF (81, 54) = 27 Find LCM (81, 54)

Q.5 Prove that $\sqrt{11}$ is an irrational number.